

**Discussion of**  
"A model of the Reserve Asset", by  
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Columbia Safe Assets Conference

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- ▶ **Two important assumptions:**
  - ▶ Rollover risk  $\Rightarrow$  Strategic complementarities
  - ▶ Fixed demand for safety  $\Rightarrow$  Strategic substitutabilities

# Review of the model

## Environment

- ▶ Two countries,  $i = 1, 2$ 
  - ▶ Supply of (unit face value) bonds:  $s_1, s_2$ , with prices  $p_1, p_2$
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- ▶ Paper: public and private signals about  $\theta_1 - \theta_2$ 
  - ▶ Threshold equilibrium
  - ▶ Non-monotone equilibrium

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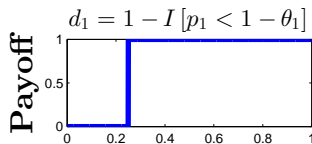
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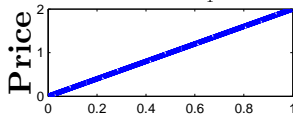
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  - ▶ Threshold equilibrium
  - ▶ Non-monotone equilibrium
- ▶ Discussion: **common knowledge**
  - ▶ Do we need the specific information structure?

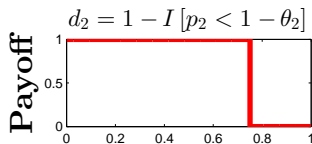
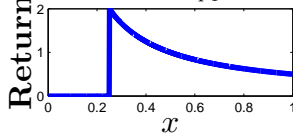
# Characterizing equilibria



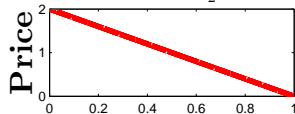
$$p_1 = \frac{(1+f)x}{s_1}$$



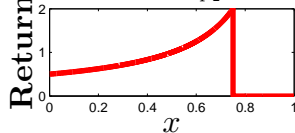
$$R_1 = \frac{d_1}{p_1}$$



$$p_2 = \frac{(1+f)(1-x)}{s_2}$$

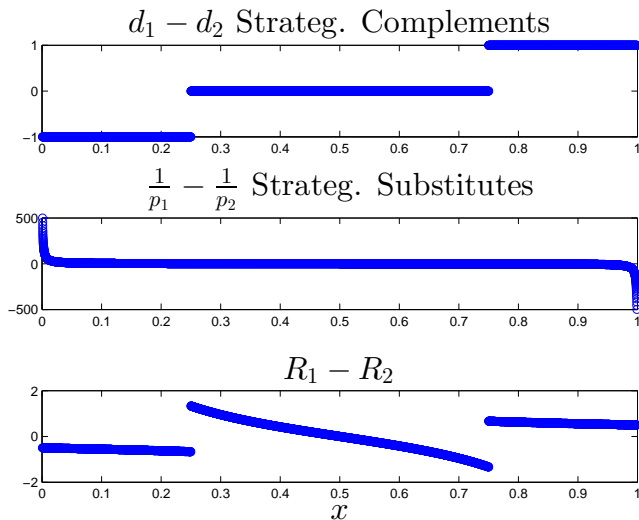


$$R_2 = \frac{d_2}{p_2}$$



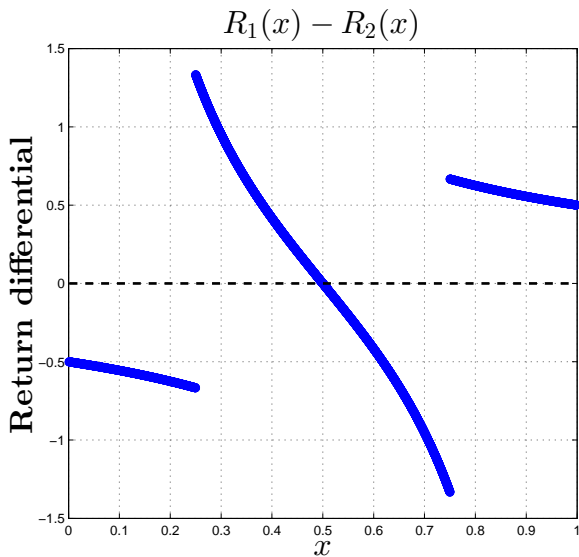
- ▶  $x \equiv$  fraction of investors that buy country 1 bond
- ▶  $s_1 = s_2 = 1$ ,  $\theta_1 = \theta_2 = 0.5$ ,  $f = 1$  (symmetric case)

# Characterizing equilibria



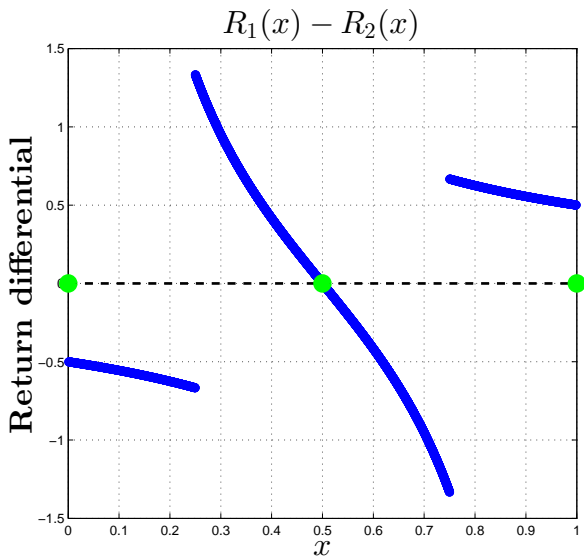
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## Common knowledge equilibria



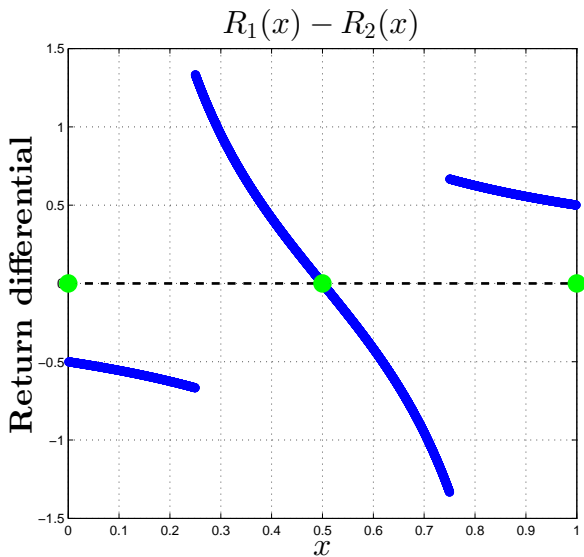
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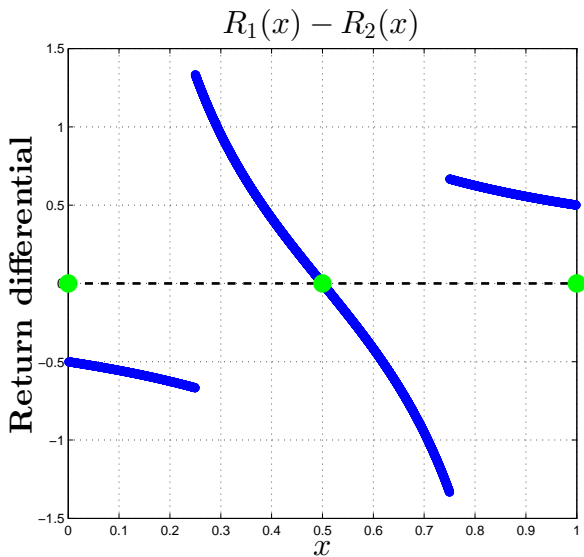
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## Common knowledge equilibria



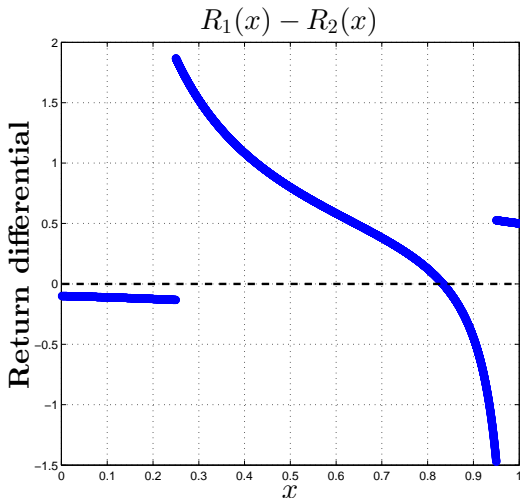
- ▶ Three **stable**, Pareto ranked equilibria
- ▶ a.e. substitutability, "overall" complementarities

# Main results in the paper

- ▶ Country 1 more likely to be reserve asset when:
  1.  $\downarrow s_2$  or  $\uparrow s_1$ : Country 1 is relatively large
  2.  $\uparrow f$  or  $\uparrow \theta$ : Savings glut or healthy global economy
  3.  $\theta_1 > \theta_2$ : Country 1 is doing well
- ▶ Why? How are equilibria affected?
- ▶ Will the results on endogenous choice of size and coordination still hold using sunspots?

## Comparative statics: **Country 2 small**

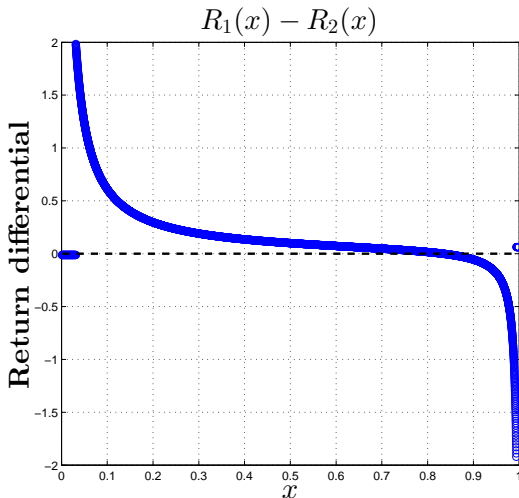
- **Thresholds:**  $\underline{x} = s_1 \frac{1-\theta_1}{1+f}$ ,  $x^* = \frac{s_1}{s_1+s_2}$ ,  $\bar{x} = 1 - s_2 \frac{1-\theta_2}{1+f}$



- Country 2 small:  $s_1 = 1$ ,  $s_2 = \mathbf{0.2}$ ,  $\theta_1 = \theta_2 = 0.5$ ,  $f = 1$

## Comparative statics: Savings glut/Healthy economy

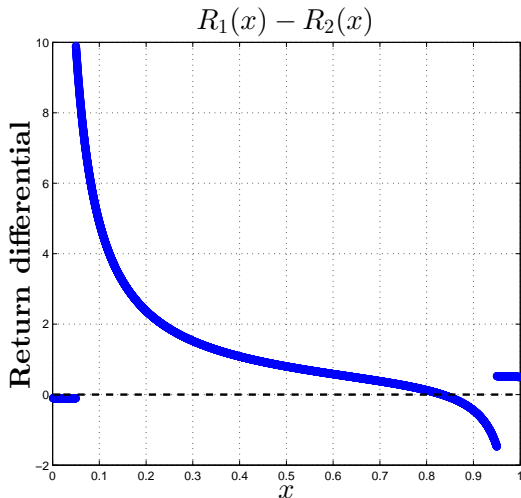
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- Savings glut  $f$  high:  $s_1 = 1$ ,  $s_2 = 0.2$ ,  $\theta_1 = \theta_2 = 0.5$ ,  $f = 15$

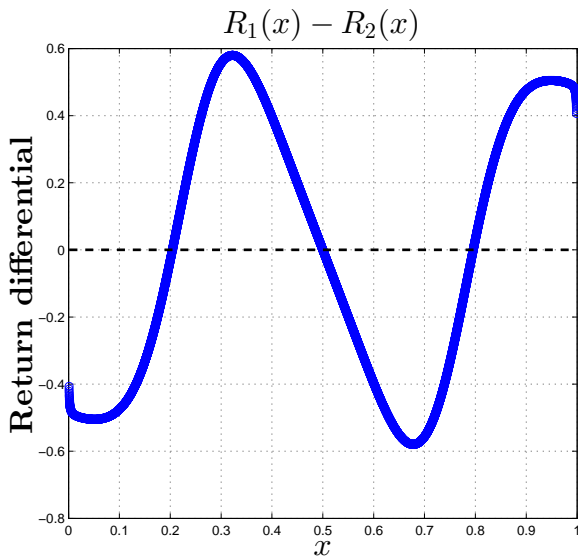
## Comparative statics: **Country 1 doing well**

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- Country 2 small:  $s_1 = 1$ ,  $s_2 = 0.2$ ,  $\theta_1 = 0.9$ ,  $\theta_2 = 0.5$ ,  $f = 1$

## Common knowledge equilibria with public signals on $\theta_1, \theta_2$



- ▶ Information smooths effects out
- ▶ Five equilibria (2 unstable)

# Conclusion

## 1. Final comments

- ▶ Bonds are denominated in real terms
  - ▶ Currency risk for bonds
  - ▶ Reserve currency
- ▶ How different are rollover risk complementarities from thick market complementarities?
- ▶ Can rollover risk based theories be used to explain the reserve status of assets in positive net supply (e.g. gold)?

## 2. Very interesting paper: lots to explore